

Helmholtzova i Gibbsova energija

Helmholtzova energija: $A = U - TS$ (T i $V = \text{konst.}$)

Gibbsova energija: $G = H - TS$ (T i $p = \text{konst.}$)

$$dA = dU - TdS$$

$$dG = dH - TdS$$

Proces unutar sustava se odvija spontano ako je:

$$dA_{T,V} \leq 0$$

$$dG_{T,p} \leq 0$$

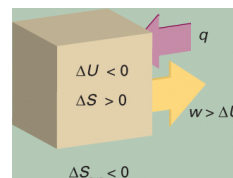
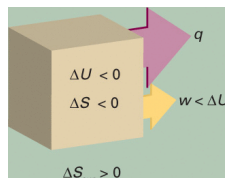
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Helmholtzova energija

Promjena Helmholtzove funkcije (funkcije maksimalnog rada) za neki proces jednaka je najvećem iznosu rada koji se može dobiti u tom procesu pri konstantnoj temperaturi i volumenu.

$$dw_{\max} = dA$$

$$w_{\max} = \Delta A = \Delta U - T\Delta S$$



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Gibbsova energija

Promjena Gibbsove funkcije (slobodne energije) jednaka je najvećem iznosu dodatnog (neekspanzijskog) rada koji se može dobiti u tom procesu pri konstantnom tlaku i temperaturi.

Kemijske reakcije se odvijaju spontano u onom smjeru u kojem se Gibbsova energija smanjuje.

$$dw_{\max} = dG$$

$$w_{\max} = \Delta G = \Delta H - T\Delta S$$

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Std. reakcijska Gibbsova energija

$$\Delta_r G^\circ = \Delta_r H^\circ - T\Delta_r S^\circ$$

$$\Delta_r G^\circ = \sum_{\text{produkti}} \nu \Delta_f G^\circ - \sum_{\text{reaktanti}} \nu \Delta_f G^\circ$$

$$\Delta_r G^\circ = \sum_j \nu_j \Delta_f G^\circ (\text{J})$$

	$\Delta_f G^\circ / (\text{kJ mol}^{-1})$
Diamond, C(s)	+2.9
Benzene, C ₆ H ₆ (l)	+124.3
Methane, CH ₄ (g)	-50.7
Carbon dioxide, CO ₂ (g)	-394.4
Water, H ₂ O(l)	-237.1
Ammonia, NH ₃ (g)	-16.5
Sodium chloride, NaCl(s)	-384.1

4 * More values are given in the Data section.

Temeljna (fundamentalna) jednačba

Dolazi iz prvog i drugog zakona termodinamike i pokazuje da je unutarnja energija zatvorenog sustava funkcija reverzibilne ili ireverzibilne promjene volumena i entropije sustava.

$$dU = TdS - pdV$$

Maxwellove jednačbe:

From U:	$\left(\frac{\partial T}{\partial V}\right)_S = -\left(\frac{\partial p}{\partial S}\right)_V$
From H:	$\left(\frac{\partial T}{\partial p}\right)_S = \left(\frac{\partial V}{\partial S}\right)_p$
From A:	$\left(\frac{\partial p}{\partial T}\right)_V = \left(\frac{\partial S}{\partial V}\right)_T$
From G:	$\left(\frac{\partial V}{\partial T}\right)_p = -\left(\frac{\partial S}{\partial p}\right)_T$

$$dU = \left(\frac{\partial U}{\partial S}\right)_V dS + \left(\frac{\partial U}{\partial V}\right)_S dV$$

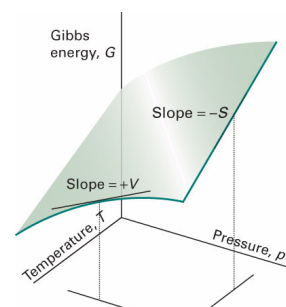
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Svojstva Gibbsove energije

Temeljna jednačba kemijske termodinamike:

$$dG = Vdp - SdT$$

$$dG = \left(\frac{\partial G}{\partial p}\right)_T dp + \left(\frac{\partial G}{\partial T}\right)_p dT$$



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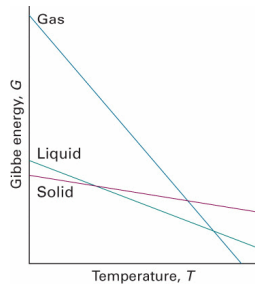
Ovisnost G o temperaturi

$$\left(\frac{\partial G}{\partial T}\right)_p = \frac{G - H}{T}$$

Gibbs-Helmholtzova jednačba:

$$\left(\frac{\partial(G/T)}{\partial T}\right)_p = -\frac{H}{T^2}$$

$$\left(\frac{\partial(\Delta G/T)}{\partial T}\right)_p = -\frac{\Delta H}{T^2}$$



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Ovisnost G o tlaku

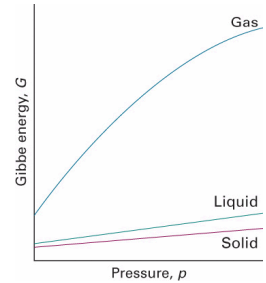
$$G_m(p_f) = G_m(p_i) + \int_{p_i}^{p_f} V_m dp$$

Za tekućine i krutine:

$$G_m(p_f) = G_m(p_i) + (p_f - p_i)V_m$$

Za idealni plin:

$$G_m(p_f) = G_m(p_i) + RT \ln \frac{p_f}{p_i}$$



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Fugacitet

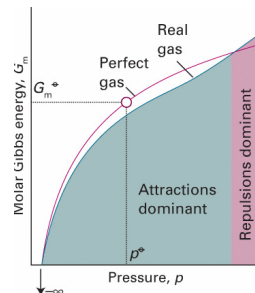
$$f = \phi p$$

Za idealni plin:

$$G_m(p) = G_m^\ominus + RT \ln \frac{p}{p^\ominus}$$

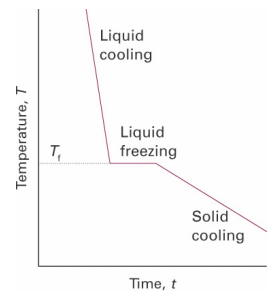
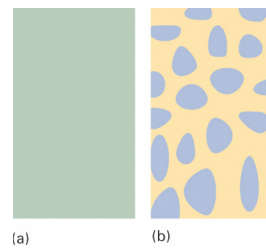
Za realni plin:

$$G_m(p) = G_m^\ominus + RT \ln \frac{f}{p^\ominus}$$



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Fizičke transformacije čistih tvari

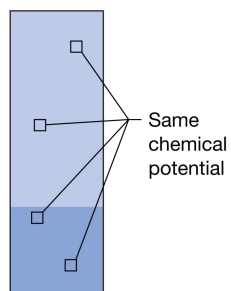


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Faze u ravnoteži

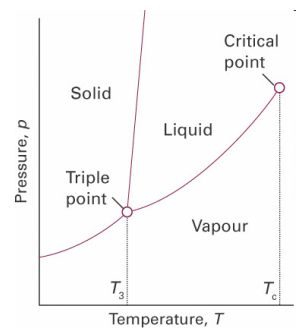
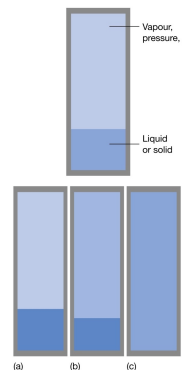
U faznoj ravnoteži, kemijski potencijal čiste tvari je isti u svim dijelovima uzorka, bez obzira na broj prisutnih faza.

Kemijski potencijal: $\mu = G_m$



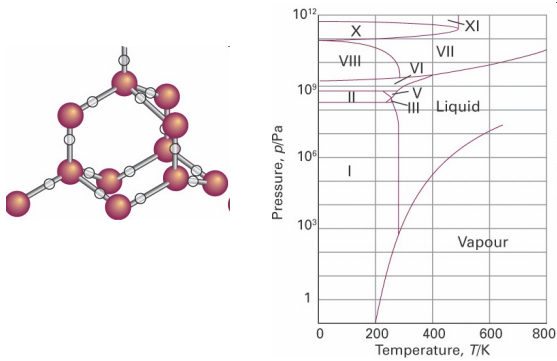
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Fazni diagram



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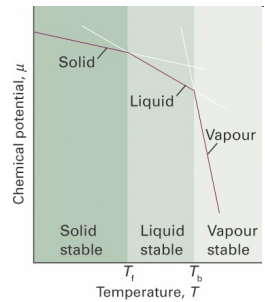
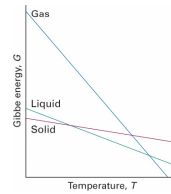
Fazni diagram vode



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Temperaturna ovisnost μ

$$\left(\frac{\partial \mu}{\partial T}\right)_p = -S_m$$

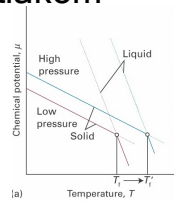


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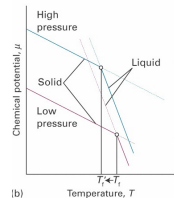
Promjena μ s tlakom

$$\left(\frac{\partial \mu}{\partial p}\right)_T = V_m$$

$$V_m(s) < V_m(l)$$



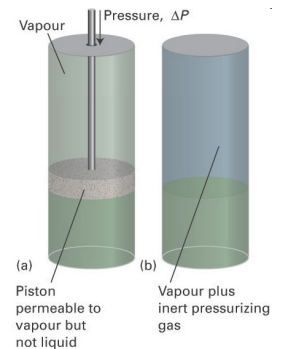
$$V_m(s) > V_m(l)$$



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Tekuća faza pod tlakom

$$p = p^* e^{\frac{V_m(l)\Delta p}{RT}}$$

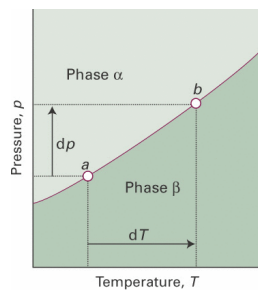


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Fazni prijelazi

Clapeyronova jednačba:

$$\frac{dp}{dT} = \frac{\Delta_{trs} S}{\Delta_{trs} V}$$

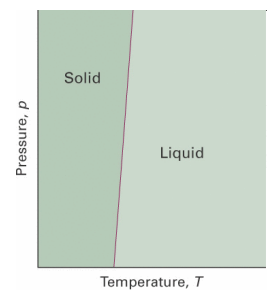


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Fazni prijelazi između s i l

$$\frac{dp}{dT} = \frac{\Delta_{fus} H}{T \Delta_{fus} V}$$

$$p = p^* + \frac{\Delta_{fus} H}{T^* \Delta_{fus} V} (T - T^*)$$



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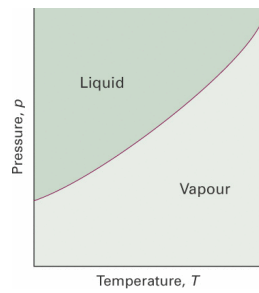
Fazni prijelazi između *l* i *g*

$$\frac{dp}{dT} = \frac{\Delta_{vap}H}{T\Delta_{vap}V}$$

Clausius-Clapeyronova
jednadžba:

$$\frac{d \ln p}{dT} = \frac{\Delta_{vap}H}{RT^2}$$

$$p = p^* e^{-\frac{\Delta_{vap}H}{R} \left(\frac{1}{T} - \frac{1}{T^*} \right)}$$

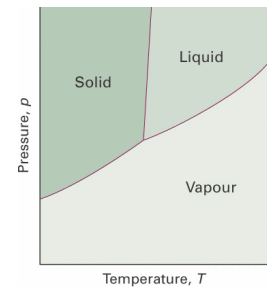


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Fazni prijelazi između *s* i *g*

$$\frac{dp}{dT} = \frac{\Delta_{sub}H}{T\Delta_{sub}V}$$

$$p = p^* e^{-\frac{\Delta_{sub}H}{R} \left(\frac{1}{T} - \frac{1}{T^*} \right)}$$



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